Arithmetic Expressions Lesson #1 Outline

1. Arithmetic Expressions Lesson #1 Outline
2. A Less Simple C Program #1
3. A Less Simple C Program #2
4. A Less Simple C Program #3
5. A Less Simple C Program #4
6. A Less Simple C Program: Compile & Run
7. Flowchart for my_add.c
8. Named Constant Example Program
9. Named Constant Example Program
10. 1997 Tax Program with Named Constants
11. What is an Expression? #1
12. What is an Expression? #2
13. What is an Expression? #3
14. What is an Expression? #4
15. What is an Expression? #5
16. What is an Expression? #6
17. What is an Arithmetic Expression? #1
18. What is an Arithmetic Expression? #2
19. What is an Arithmetic Expression? #3
20. Arithmetic Expression Examples
22. Arithmetic Operations
23. Structure of Arithmetic Expressions #1
24. Structure of Arithmetic Expressions #2
25. int-valued & float-valued Expressions
26. Precedence Order
27. Precedence Order Examples
28. Precedence Order Example: int #1
29. Precedence Order Example: int #2
30. Precedence Order Example: float #1
31. Precedence Order Example: float #2
#include <stdio.h>

int main ()
{
   /* main */
   
   const int program_success_code = 0;
   
   int addend, augend, sum;

   /* main */
   
   printf("Enter two integers: ");
   scanf("%d %d", &addend, &augend);

   sum = addend + augend;
   printf("The sum is: %d\n", sum);

   return program_success_code;
}
A Less Simple C Program #2

/*
 ****************************
 *** Execution Section ***
 ****************************
*/

Greeting Subsection *

* Tell the user what the program does.
*/
printf("I'll add a pair of integers.\n");

Input subsection *

* Prompt the user to input the addend & augend.
*/
printf("What pair of integers do you want to add?\n");

* Input the integers to be added.
*/
scanf("%d %d", &addend, &augend);

Continued on the next slide.
The statement as a whole is an **assignment statement**.
The stuff to the right of the single equals sign is an **arithmetic expression**.
#include <stdio.h>

int main ()
{ /* main */
    const int program_success_code = 0;
    int addend, augend, sum;

    printf("I'll add a pair of integers.\n");
    printf("What pair of integers do you want to add?\n");
    scanf("%d %d", &addend, &augend);
    sum = addend + augend;
    printf("The sum of %d and %d is %d.\n", addend, augend, sum);
    return program_success_code;
} /* main */

The statement as a whole is an assignment statement.
The stuff to the right of the single equals sign is an arithmetic expression.
% gcc -o my_add my_add.c
% my_add
I'll add a pair of integers.
What pair of integers do you want to add? 5 7
The sum of 5 and 7 is 12.
% my_add
I'll add a pair of integers.
What two integers do you want to add? 1593 09832
The sum of 1593 and 9832 is 11425.
Flowchart for my_add.c

Start

Output a description of the program.

Prompt the user to input the addend and augend.

Input the addend and augend.

Add addend to augend and store the result in sum.

Output the sum.

End

A rectangle denotes an operation other than I/O or branching (for example, calculation).
Named Constant Example Program

% cat circlecacalc.c
#include <stdio.h>
int main ()
{
    const float pi = 3.1415926;
    const float diameter_factor = 2.0;
    const int program_success_code = 0;
    float radius, circumference, area;

    printf("I'm going to calculate a circle's\n");
    printf(" circumference and area.\n");
    printf("What's the radius of the circle?\n");
    scanf("%f", &radius);
    
    circumference = pi * radius * diameter_factor;
    area = pi * radius * radius;
    printf("The circumference is %f\n", circumference);
    printf(" and the area is %f.\n", area);
    return program_success_code;
}

% gcc -o circlecacalc circlecacalc.c
% circlecacalc
I'm going to calculate a circle's circumference and area.
What's the radius of the circle?
5
The circumference is 31.415924
and the area is 78.539810.
Named Constant Example Program

% cat circlecalc.c
#include <stdio.h>
int main ()
{ /* main */
    const float pi                   = 3.1415926;
    const float diameter_factor = 2.0;
    const int  program_success_code = 0;
    float radius, circumference, area;

    printf("I'm going to calculate a circle's\n");
    printf(" circumference and area.\n");
    printf("What's the radius of the circle?\n");
    scanf("%f", &radius);
    circumference = pi * radius * diameter_factor;
    area = pi * radius * radius;
    printf("The circumference is %f\n", circumference);
    printf(" and the area is %f.\n", area);
    return program_success_code;
} /* main */
%
% gcc -o circlecalc circlecalc.c
% circlecalc
I'm going to calculate a circle's circumference and area.
What's the radius of the circle? 5
The circumference is 31.415924 and the area is 78.539810.
% cat tax1997_named.c
#include <stdio.h>

int main ()
{ /* main */
    const float standard_deduction = 4150.0;
    const float single_exemption = 2650.0;
    const float tax_rate = 0.15;
    const int tax_year = 1997;
    const int program_success_code = 0;
    float income, tax;

    printf("I'm going to calculate the federal income tax\n");
    printf(" on your %d income.\n", tax_year);
    printf("What was your %d income in dollars?\n", tax_year);
    scanf("%f", &income);

    tax = (income - (standard_deduction + single_exemption)) * tax_rate;
    printf("The %d federal income tax on $%2.2f\n", tax_year, income);
    printf(" was $%2.2f.\n", tax);
    return program_success_code;
} /* main */

% gcc -o tax1997_named tax1997_named.c
% tax1997_named
I'm going to calculate the federal income tax
 on your 1997 income.
What was your 1997 income in dollars?
20000
The 1997 federal income tax on $20000.00
was $1980.00.
What is an Expression? #1

\( a + b - c * d / e \% f - (398 + g) * 5981 / 15 \% h \)

In programming, an *expression* is a combination of:

- **Operands**
- **Operators**
- **Parentheses**: (  )

Not surprisingly, an expression in a program can look very much like an expression in math (though not necessarily identical). This is on purpose.

**NOTE**: In C, the only characters you can use for parenthesizing are *actual parentheses* (unlike in math, where you can also use square brackets and curly braces as well.)
What is an Expression? #2

\[ a + b - c \times d / e \% f - (398 + g) \times 5981 / 15 \% h \]

In programming, an **expression** is a combination of:

- **Operands**, such as:
  - Literal constants
  - Named constants
  - Variables
  - **Function invocations** (which we’ll discuss later)

- **Operators**

- **Parentheses**: ( )
What is an Expression? #3

In programming, an *expression* is a combination of:

- **Operands**
- **Operators**, such as:
  - Arithmetic Operators
  - Relational Operators
  - Logical Operators
- **Parentheses**: ( )

\[ a + b - c \times d \div e \% f - (398 + g) \times 5981 \div 15 \% h \]
What is an Expression? #4

a + b - c * d / e % f - (398 + g) * 5981 / 15 % h

In programming, an expression is a combination of:

- **Operands**
- **Operators**, such as:
  - Arithmetic Operators
    - Addition: +
    - Subtraction: -
    - Multiplication: *
    - Division: /
    - **Modulus** (remainder): % (only for int operands)
  - Relational Operators
  - Logical Operators
- **Parentheses**: (  )
What is an Expression? #5

In programming, an *expression* is a combination of:

- **Operands**
- **Operators**, such as:
  - Arithmetic Operators
  - Relational Operators
    - Equal: `==`
    - Not Equal: `!=`
    - Less Than: `<`
    - Less Than or Equal To: `<=`
    - Greater Than: `>`
    - Greater Than or Equal To: `>=`
  - Logical Operators
- **Parentheses**: `( )`
What is an Expression? #6

In programming, an expression is a combination of:

- **Operands**
- **Operators**, such as:
  - Arithmetic Operators
  - Relational Operators
  - Logical Operators
    - **Negation** (NOT): !
    - **Conjunction** (AND): &&
    - **Disjunction** (OR): ||
  - Parentheses: ( )

We’ll learn about these later.
What is an Arithmetic Expression? #1

An *arithmetic expression* (also called a *numeric expression*) is a combination of:

- **Numeric operands**
- **Arithmetic Operators**
- **Parentheses**: (  )
What is an Arithmetic Expression? #2

An *arithmetic expression* (also called a *numeric expression*) is a combination of:

- **Numeric operands**, such as:
  - int & float literal constants (BAD BAD BAD)
  - int & float named constants (GOOD)
  - int & float variables
  - int-valued & float-valued *function invocations*

- **Arithmetic Operators**

- **Parentheses**: (  )
What is an Arithmetic Expression? #3

An *arithmetic expression* (also called a *numeric expression*) is a combination of:

- **Numeric operands**
- **Arithmetic Operators**, such as:
  - Identity: +
  - Negation: −
  - Addition: +
  - Subtraction: −
  - Multiplication: *
  - Division: /
  - *Modulus* (remainder): % (only for *int* operands)
- **Parentheses**: (  )
Arithmetic Expression Examples

\[ x \]
\[ +x \]
\[ -x \]
\[ x + y \]
\[ x - y \]
\[ x \times y \]
\[ x \div y \]
\[ x \% y \]
\[ x + y - (z \% 22) \times 7 \div \cos(\theta) \]
Arithmetic operations come in two varieties: **unary** and **binary**.

A **unary operation** is an operation that has only one operand. For example:

\[-x\]

Here, the **operand** is \(x\), the **operator** is the minus sign, and the **operation** is negation.

A **binary operation** uses two operands. For example:

\[y + z\]

Here, the **operands** are \(y\) and \(z\), the **operator** is the plus sign, and the **operation** is addition.
### Arithmetic Operations

<table>
<thead>
<tr>
<th>Operation</th>
<th>Kind</th>
<th>Operator</th>
<th>Usage</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Identity</td>
<td>Unary</td>
<td>+</td>
<td>+x</td>
<td>Value of x</td>
</tr>
<tr>
<td></td>
<td></td>
<td>none</td>
<td>x</td>
<td>Value of x</td>
</tr>
<tr>
<td>Negation</td>
<td>Unary</td>
<td>−</td>
<td>−x</td>
<td>Additive inverse of x</td>
</tr>
<tr>
<td>Addition</td>
<td>Binary</td>
<td>+</td>
<td>x + y</td>
<td>Sum of x and y</td>
</tr>
<tr>
<td>Subtraction</td>
<td>Binary</td>
<td>−</td>
<td>x − y</td>
<td>Difference between x and y</td>
</tr>
<tr>
<td>Multiplication</td>
<td>Binary</td>
<td>*</td>
<td>x * y</td>
<td>Product of x times y (i.e., x • y)</td>
</tr>
<tr>
<td>Division</td>
<td>Binary</td>
<td>/</td>
<td>x / y</td>
<td>Quotient of x divided by y</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>(i.e., x ÷ y)</td>
</tr>
<tr>
<td>Modulus</td>
<td>Binary</td>
<td>%</td>
<td>x % y</td>
<td>Remainder of x divided by y</td>
</tr>
<tr>
<td>(int only)</td>
<td></td>
<td></td>
<td></td>
<td>(that is, x - [x ÷ y] • y)</td>
</tr>
</tbody>
</table>
Structure of Arithmetic Expressions #1

An arithmetic expression can be long and complicated. For example:

```
a + b - c * d / e % f
```

*Terms* and *operators* can be mixed together in almost limitless variety, but they must follow the rule that a unary operator has a term immediately to its right and a binary operator has terms on both its left and its right:

```
-a + b - c * d / e % f - (398 + g) * 5981 / 15 % h
```

*Parentheses* can be placed around any unary or binary subexpression:

```
((-a) + b - c) * d / e % f - ((398 + g) * 5981 / 15) % h
```
Structure of Arithmetic Expressions #2

Putting a term in **parentheses** may change the value of the expression, because a term inside parentheses will be **calculated first**.

For example:

\[ a + b \times c \]

is evaluated as

“multiply \( b \) by \( c \), then add \( a \),” but

\[(a + b) \times c\]

is evaluated as

“add \( a \) and \( b \), then multiply by \( c \)”

**Note**: As a general rule, you **cannot** put two operators in a row (but we’ll see exceptions, sort of).
int-valued & float-valued Expressions

An **int-valued expression** is an expression that, when it is evaluated, has an **int** result.

A **float-valued expression** is an expression that, when it is evaluated, has a **float** result.
Precedence Order

In the absence of parentheses that explicitly state the order of operations, the *order of precedence* (also known as the *order of priority*) is:

- **first**: multiplication and division, left to right, and then
- **second**: addition, subtraction, identity and negation, left to right.

After taking into account the above rules, the expression as a whole is evaluated left to right.
Precedence Order Examples

- $1 - 2 - 3 = -1 - 3 = -4$ but
  $1 - (2 - 3) = 1 - (-1) = 2$

- $1 + 2 * 3 + 4 = 1 + 6 + 4 = 7 + 4 = 11$ but
  $(1 + 2) * 3 + 4 = 3 * 3 + 4 = 9 + 4 = 13$

- $24 / 2 * 4 = 12 * 4 = 48$ but
  $24 / (2 * 4) = 24 / 8 = 3$

- $5 + 4 \% 6 / 2 = 5 + 4 / 2 = 5 + 2 = 7$ but
  $5 + 4 \% (6 / 2) = 5 + 4 \% 3 = 5 + 1 = 6$ but
  $(5 + 4) \% (6 / 2) = 9 \% (6 / 2) = 9 \% 3 = 0$

**Rule of Thumb**: If you can’t remember the precedence order of the operations, use lots of parentheses.

But **DON’T** overdo your use of parentheses, because then your code would be “write only.”
Precedence Order Example: int #1

#include <stdio.h>

int main ()
{
    /* main */
    printf("1 - 2 - 3 = %d\n", 1 - 2 - 3);
    printf("1 - (2 - 3) = %d\n", 1 - (2 - 3));
    printf("\n");
    printf("1 + 2 * 3 + 4 = %d\n", 1 + 2 * 3 + 4);
    printf("(1 + 2) * 3 + 4 = %d\n", (1 + 2) * 3 + 4);
    printf("\n");
    printf("24 / 2 * 4 = %d\n", 24 / 2 * 4);
    printf("24 / (2 * 4) = %d\n", 24 / (2 * 4));
    printf("\n");
    printf("5 + 4 % 6 / 2 = %d\n", 5 + 4 % 6 / 2);
    printf("5 + 4 % (6 / 2) = %d\n", 5 + 4 % (6 / 2));
    printf("(5 + 4) % (6 / 2) = %d\n", (5 + 4) % (6 / 2));
}

Notice that a printf statement CAN output the value of an expression (but that’s usually NOT RECOMMENDED).
Precedence Order Example: int  #2

% gcc -o int_expressions int_expressions.c
% int_expressions
1 - 2 - 3 = -4
1 - (2 - 3) = 2

1 + 2 * 3 + 4 = 11
(1 + 2) * 3 + 4 = 13

24 / 2 * 4 = 48
24 / (2 * 4) = 3

5 + 4 % 6 / 2 = 7
5 + 4 % (6 / 2) = 6
(5 + 4) % (6 / 2) = 0
#include <stdio.h>

int main ()
{ /* main */
    printf("1.0 - 2.0 - 3.0 = %f\n", 1.0 - 2.0 - 3.0);
    printf("1.0 - (2.0 - 3.0) = %f\n", 1.0 - (2.0 - 3.0));
    printf("\n");
    printf(" 1.0 + 2.0 * 3.0 + 4.0 = %f\n", 1.0 + 2.0 * 3.0 + 4.0);
    printf("(1.0 + 2.0) * 3.0 + 4.0 = %f\n", (1.0 + 2.0) * 3.0 + 4.0);
    printf("\n");
    printf("24.0 / 2.0 * 4.0 = %f\n", 24.0 / 2.0 * 4.0);
    printf("24.0 / (2.0 * 4.0) = %f\n", 24.0 / (2.0 * 4.0));
} /* main */

Again, notice that a printf statement CAN output the value of an expression (but that’s usually NOT RECOMMENDED).
Precendence Order Example: float #2

% gcc -o real_expressions real_expressions.c
% real_expressions
1.0 - 2.0 - 3.0 = -4.000000
1.0 - (2.0 - 3.0) = 2.000000

1.0 + 2.0 * 3.0 + 4.0 = 11.000000
(1.0 + 2.0) * 3.0 + 4.0 = 13.000000

24.0 / 2.0 * 4.0 = 48.000000
24.0 / (2.0 * 4.0) = 3.000000